

Application: Sieve of Eratosthenes

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CMPT14x

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List operations (Python)

```
myApples = [ "Fuji", "Gala", "Red Delicious" ]
```

- Test for list membership:

```
if "Fuji" in myApples: # True
```

- Concatenate:

```
[ 'a', 'b', 'c' ] + [ 'd', 'e' ]
```

- Repeat:

```
[ 'a', 'b', 'c' ] * 2
```

- Modify list entries (mutable):

```
myApples[1] = "Braeburn"
```

- Convert a string to a list of characters:

```
list("Hello World!") # ['H', 'e', 'l', 'l', 'o', ...]
```

More list operations

- **Delete** an element of the list:

```
del myApples[1]      # [ "Fuji", "Golden Delicious" ]
```

- List **slice** (start:end):

```
myApples[0:1]      # [ "Fuji", "Gala" ]
```

- Assignment is **aliasing**:

```
yourApples = myApples      # points to same array
```

- Use a whole-list slice to **copy** a list:

```
yourApples = myApples[:]
```

```
#[:] is shorthand for [0:-1] or  
[0:len(myApples)-1]
```

Quiz 03: 10 minutes, 20 points

- Define **recursion** in your own words.
 - Write a short **example** in Python to illustrate.
 - ◆ (It doesn't have to do anything useful.)
- What is the **call stack** used for?
- What are **global variables** and why are they bad?
- Write a Python **function** that returns the sum of a given list.
 - ◆ Docstring required! Comment as appropriate.
 - ◆ Error-checking or pre-conditions required

Quiz 03: answers #1-2

- What is **recursion**?

- A recursive function invokes itself:

```
def countdown(n):
```

```
    if n <= 0:
```

```
        return 0
```

```
    print n,
```

```
    return countdown(n-1)
```

- What is the **call stack**?

- Keeps track of which procedures are currently running. Made up of stack frames, recording local variables and parameters for each function invocation.

Quiz 03: answers #3-4

- What are **global** variables?
 - Accessible everywhere in the module: even inside functions defined in the module
 - Functions can modify global variables and cause unintended side-effects
- Calculate the sum of a list:

```
def sum(vec):
```

```
    """Sum the input list.
```

```
    Vec must be a list of ints or floats."""
```

```
    result = 0.0
```

```
    for term in vec:
```

```
        result += term
```

```
    return result
```

Sieve of Eratosthenes

- **Problem**: list all the **prime** numbers between 2 and some given big number.
 - You had a **homework** that was similar: test if a given number is prime, and list its factors
 - How did you solve that?
 - ◆ Procedure **is_prime()** (pseudocode):
Iterate for factor in 2 .. sqrt(n):
If (n % factor == 0), then
We've found a factor!
- But this is wasteful: really only need to test **prime** numbers for potential factors

Listing all primes

- We could tackle this problem by repeatedly calling `is_prime()` on **every** number in turn:

```
for num in range(2, max):  
    if is_prime(num) ...
```
- But this could be really **slow** if **max** is big
- Is there a smarter way to eliminate **non-prime** (composite) numbers?

Sieve of Eratosthenes

- The sieve works by a process of **elimination**: we eliminate all the **non-primes** by turn:



Prime sieve: pseudocode

- 1) Create an **array** of booleans and set them all to **true** at first. (**true** = **prime**)
- 2) Set array element **1** to **false**. Now **2** is **prime**.
- 3) Set the values whose index in the array is a **multiple** of the last prime found to **false**.
- 4) The next index where the array holds the value **true** is the **next prime**.
- 5) Repeat steps 3 and 4 until the last prime found is greater than the **square root** of the largest number in the array.

Prime sieve: Python code

```
"""Find all primes up to a given number, using  
Eratosthenes' prime sieve."""
```

```
import math                # sqrt
```

```
size = input("Find all primes up to: ")
```

```
# Initialize: all numbers except 0, 1 are prime
```

```
primeFlags = range(size+1)    # so pF[size] exists
```

```
for num in range(size+1):
```

```
    primeFlags[num] = True
```

```
primeFlags[0] = False
```

```
primeFlags[1] = False
```

Prime sieve: Python code (p.2)

```
# Computation: eliminate all non-primes
for num in range(2, int(math.sqrt(size))+1):
    if primeFlags[num]:           # got a prime
        # Eliminate its multiples
        for multiple in range(num**2, size+1, num):
            primeFlags[multiple] = False

# Output
print "Your primes, sir/madam:",
for num in range(2, size+1):
    if primeFlags[num]:
        print num,
```

<http://twu.seanho.com/python/primesieve.py>