

# Semester Review

6 Dec 2011  
BUSI275  
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- **Paper** due tomorrow
- **Final** this Sat

# Overview: foundation

- Intro: **variables**, sampling (Ch1)
- Exploring data:
  - Via **charts** (Ch2), via **descriptives** (Ch3)
- **Probability** and independence (Ch4)
- Probability **distributions**:
  - Discrete: **binom**, **Poisson**, **hypg** (Ch5)
  - Continuous: **norm**, **unif**, **expon** (Ch6)
- **Sampling** distributions (Ch7, 8)
  - SDSM (**norm** and **t-dist**), **binomial**
  - Types of problems: **% area**, **conf. int.**, **n**
- **Hypothesis testing** (Ch9):
  - $H_0/H_A$ , **rej / fail rej**, **Type-I/II**,  $\alpha/\beta$ , **p-value**



# Overview: statistical tests

- **T-tests (Ch10):**
  - 1 sample mean (ch9)
  - Two **independent** samples (het  $\sigma$ , hom  $\sigma$ )
  - **Paired** data (Excel type 1)
- **Regression (Ch14-15):**
  - Linear model, predicted  $\hat{y}$ , residuals
  - $R^2$ , F-test, t-test on slopes, interaction
- **ANOVA (ch12):**
  - One-way + Tukey-Kramer
  - **Blocking** (w/o repl) + Fisher's LSD
  - **Two-way** (w/repl), **interaction**
- **$\chi^2$  (ch13): contingency tables, O vs. E**

# Ch2-3: Exploring Data

- For **nominal** variables:
  - Charts: **bar/col, pie**
    - ◆ Joint distrib of **2 vars**: **pivot** table
  - Stats: **frequency** distribution
- For **scale** (quantitative) (interval/ratio) vars:
  - Charts: **histogram, ogive (cum), boxplot**
    - ◆ **2 vars**: **scatter**
    - ◆ **Time series**: **line**
  - Centre: **mean, median, mode**, (skew)
  - Quantile:  **$Q_1/Q_3$ , %ile, IQR**
  - Std dev:  **$\sigma, s, CV$ , empirical rule, z-score**

# Ch4: Probability

- Tree diagrams
- $P(A)$  notation, Venn diagrams
  - Sample space, outcome, event
  - $n$ ,  $U$ , complement
- Addition rule:  $A \cup B = A + B - (A \cap B)$ 
  - Mutual exclusivity
- Conditional probability
  - What does it mean; how to find it (Bayes)
  - Statistical independence
    - ◆ Does  $P(A|B) = P(A)$  ?

# Ch5: Discrete distributions

- Binomial: BINOM(x, n, p, cum)
  - x: counting # of successes out of n trials
  - p: probability of success (binom proportion)
- Poisson: POISSON(x,  $\lambda$ , cum)
  - x: # occurrences within the time period
  - $\lambda$ : mean (expected) # occ w/in the period
- Hypergeometric: HYPGEOMDIST(X, N, x, n)
  - X, N: # successes & tot size of population
    - ◆ Binomial  $p = X/N$
  - x, n: # successes & tot size of sample

# Ch6: Continuous distributions

- Normal: NORMDIST( $x$ ,  $\mu$ ,  $\sigma$ , cum)
  - Also NORMINV(area,  $\mu$ ,  $\sigma$ ),  
NORMSDIST( $z$ ), NORMSINV(area)
- Uniform:
  - $P(x) = 1/(b-a)$ ,  $\mu = (a+b)/2$ ,  $\sigma = \sqrt{((b-a)^2/12)}$
- Exponential: EXPONDIST( $x$ ,  $\lambda$ , cum)
  - $x$ : time between occurrences
  - $\lambda$ : 1 / (mean time between occurrences)
    - ◆  $\lambda$  = expected frequency of occurrences  
(e.g., occurrences per min)

# Ch7-8: Sampling distributions

- Sampling distributions:
  - SDSM, w/ $\sigma$ : NORMDIST(), SE =  $\sigma/\sqrt{n}$
  - SDSM, w/ $s$ : TDIST(), SE =  $s/\sqrt{n}$
  - Binomial proportion: norm, SE =  $\sqrt{(pq / n)}$
- Types of problems: area,  $\mu$ , thresh, n,  $\sigma$ 
  - Area: prob of getting a sample in given range
  - Threshold: e.g., confidence interval
  - n: minimum sample size



# Ch9: Hypothesis testing

- Decision making
- $H_0$  vs.  $H_A$ , in words and notation (e.g.,  $\mu_1 \neq \mu_2$ )
- Conclusions: reject  $H_0$  vs. fail to reject  $H_0$
- Risks/errors: Type-I vs. Type-II
  - Level of significance:  $\alpha$
  - Power:  $1-\beta$
- p-value: what is it, how do we use it?

# Ch10: t-tests

- T-test on **1** sample (ch8-9):
  - SDSM:  $SE = s/\sqrt{n}$
  - Binomial proportions:  $SE = \sqrt{(pq/n)}$
- T-test on **two independent** samples, general:
  - $SE = \sqrt{(SE_1^2 + SE_2^2)}$ ,  $df = \text{complicated}$
- T-test on **two independent** samples, **similar  $\sigma$** :
  - $SE = s_p \sqrt{(1/n_1 + 1/n_2)}$ ,  $df = df_1 + df_2$
- T-test on two **proportions**:
  - $SE = \sqrt{(SE_1^2 + SE_2^2)}$ , use **z** instead of t
- T-test on **paired** data:
  - $SE = s_d / \sqrt{n}$ ,  $df = (\#pairs) - 1$

# Ch14-15: Regression

- Scatter plots and correlation, t-test on  $r$ 
  - $R^2$  and % variability explained
- Linear model  $Y = b_0 + b_1X + \varepsilon$ 
  - Finding+interpreting slope+intercept
  - Finding+interpreting  $s_\varepsilon$  (STEYX)
- Assumptions / diagnostics:
  - Linearity + homoscedasticity (residual plots)
  - Normality of residuals (histogram)
  - (skip: non-collinearity + indep of resids)
- Multiple regression + concept of moderation

# Ch12-13: Categorical data

## ■ Ch12: ANOVA:

- $H_0 / H_A$ , global F-test, concept of follow-up
- One-way ANOVA + Tukey-Kramer
- Blocking ANOVA + Fisher's LSD
  - ◆ F-test for main factor effect
  - ◆ F-test for whether blocking is needed
- Two-way ANOVA
  - ◆ F-test for each main effect
  - ◆ F-test for interaction

## ■ Ch13: $\chi^2$ (O vs. E)

- 1 var vs. uniform, normal
- 2 vars (contingency table): independence